## BITCOIN

## A Peer-to-Peer Electronic Cash System

## Abstract. A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending.

We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of hash-based proof-of-work, forming a record that cannot be changed without redoing the proof-of-work. The longest chain not only serves as proof of the sequence of events witnessed, but proof that it came from the largest pool of CPU power. As long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpace attackers. The network itself requires minimal structure. Messages are broadcast on a best effort basis, and nodes can leave and rejoin the network at will, accepting the longest proof-of-work chain as proof of what happened while they were gone.
process electronic payments. While the system works well enough for most transactions, it still suffers from the inherent weaknesses of the trust based model. Completely mon-reversible
transactions are not really possible, since financial institutions cannot avoid mediating disputes. The cost of mediation transaction size and cutting off the possibility for small casual transactions, and there is a broader cost in the loss of ability to make non-reversible payments for non-reversible services With the possibility of reversal, the need for trust spreads. more information than they would otherwise need. A certain解centage of fraud is accepted as unavoidable. These costs
 mysical currency, but no mechanism exists to make payments needed is an electronic payment system based on cryptographic proof instead of trust, allowing any two willing parties to transact directly with each other without the need for mpractical to reverse would protect sellers from fraud, and routine escrow mechanisms could easily be implemented to protect buyers. In this paper, we propose a solution to the double-spending problem using a peer-to-peer distributed or the sentational proof of the long as honest nodes collectively control more CPU power han any cooperating group of attacker nodes
2. Transactions
We define an electronic coin as a chain of digital signatures, Each owner transfers the coin to the next by digitally signing a owner and adding these to the end of the coin. A payee can verify the signatures to verify the chain of ownership.

| Transaction |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Owner 1's Public Key |  | Owner 2's <br> Public Key |  | Owner 3's <br> Public Key |
| H Vash |  | $\underset{\text { Hash }}{\substack{\text { Hen }}}$ |  | Hash |
| $\checkmark$ | $v_{\text {eriris, }}$ | $\checkmark$ | $V_{\text {erity }}$ | $\checkmark$ |
| Owner 0's Signature |  | $\begin{aligned} & \text { Owner 1's } \\ & \text { Signature } \end{aligned}$ |  | Owner 2's |
|  | gis |  | gis |  |
| Owner 1's Private Key |  | Owner 2's <br> Private Key |  | Owner 3's <br> Private Key |

The problem of course is the payee can't verify that one of the owners did not double-spend the coin. A common solution is every transaction for double spending. After each transaction, he coin must be returned to the mint to issue a new coin, and only coins issued directly from the mint are trusted not to be the entire money system depends on the company running the mint, with every transaction having to go through them, just like a bank. We need a way for the payee to know that the previous owners did not sign any earlier transactions. For our purposes, the earliest transaction is the one that counts, so we don't care about later attempts to double-spend. The only all transactions. In the mint based model the mint was aware all transactions. In the mint based model, the mint was aware accomplish this without a trusted party, transactions must be publicly announced [1], and we need a system for participants to agree on a single history of the order in which they were received. The payee needs proof that at the time of each
transaction, the majority of nodes agreed it was the first transaction
received.
3. Timestamp Server

The solution we propose begins with a timestamp server. A
timestamp server works by taking a hash of a block of items to mestamp server works by taking a hash of a block of items to newspaper or Usenet post [2-5]. The timestamp proves that the data must have existed at the time, obviously, in order to get into the hash. Each timestamp includes the previous
timestamp in its hash, forming a chain, with each additional timestamp in its hash, forming a chain, with each additiona

| - Hash | Hash |
| :---: | :---: |
| Block | Block |

## 4. Proof-of-Work

To implement a distributed timestamp server on a peer-to-pee dasis, we will need to use a proof- of-work system similar to posts. The proof-of-work involves scanning for a value that when hashed, such as with SHA-256, the hash begins with a number of zero bits. The average work required is exponential
in the number of zero bits required and can be verified by executing a single hash. For our timestamp network, we implement the proof-of-work by incrementing a nonce in the block until a value is found that gives the block's hash the required zero bits. Once the CPU effort has been expended to make it satisfy the proof-of-work, the block cannot be changed without redoing the work. As later blocks are chained after it, the work to change the block would include redoing all the blocks after it.

## Block

The proof-of-work also solves the problem of determining representation in majority decision making. If the majority were
based on one-IP-address-one-vote, it could be subverted by anyone able to allocate many IPs. Proof-of-work is essentially one-CPU-one-vote. The majority decision is represented by he longest chain, which has the greatest proof-of-work effort honest nodes, the honest chain will grow the fastest and outpace any competing chains. To modify a past block, an attacker would have to redo the proof-of-work of the block and all blocks after it and then catch up with and surpass the work of the honest nodes. We will show later that the probability of slower attacker catching up diminishes exponentially as subsequent blocks are added. To compensate for increasing time, the proof-of-work difficulty is determined by a moving average targeting an average number of blocks per hour. if they're generated too fast, the difficulty increases.

## 5. Network

The steps to run the network are as follows:

1) New transactions are broadcast to all nodes.
) Each node collects new transactions into a block
2) Eack

## lock.

4) When a no
to all nodes.
5) Nodes accept the block only if all transactions in it are valid and not already spent.
6) Nodes express their acceptance of the block by working on creating the next block in the chain, using the hash of the accepted block as the previous hash.
Nodes always consider the longest chain to be the correct one different versions of the next block simultaneously, some nodes may receive one or the other first. In that case, they work on the first one they received, but save the other branch in case it becomes longer. The tie will be broken when the hext proof- of-work is found and one branch becomes longer; he nodes that were working on the other branch will then switch to the longer one. 3 New transaction broadcasts do not mecessarily need to reach all nodes. As long as they reach
many nodes, they will get into a block before long. Block broadcasts are also tolerant of dropped messages. If a node does not receive a block, it will request it when it receives the next block and realizes it missed one.
6. Incentive

By convention, the first transaction in a block is a special ransaction that starts a new coin owned by the creator of the block. This adds an incentive for nodes to support the etwork, and provides a way to initially distribute coins into The steady addition of a constant of amount of new coins is analogous to gold miners expending resources to add gold to circulation. In our case, it is CPU time and electricity that is expended. The incentive can also be funded with transaction ees. If the output value of a transaction is less than its input value, the difference is a transaction fee that is added to the predetermined number of coins have entred circulation the incentive can transition entirely to transaction fees and be completely inflation free. The incentive may help encourage nodes to stay honest. If a greedy attacker is able to assemble more CPU power than all the honest nodes, he would have to choose between using it to defraud people by stealing back his payments, or using it to generate new coins. He ought to find it more profitable to play by the rules, such rules that than to undermine the system and the validity of his own han to

## . Reclaiming Disk Space

Once the latest transaction in a coin is buried under enough blocks, the spent transactions before it can be discarded to save disk space. To facilitate this without breaking the block's hash, transactions are hashed in a Merkle Tree [7][2][5], with only the root included in the block's hash. Old blocks can then interior hashes do not need to be stored.


A block header with no transactions would be about 80 bytes, bytes * $6 * 24 * 365=42 \mathrm{mB}$ per year. With computer systems typically selling with 2 GB of RAM as of 2008, and Moore's Law predicting current growth of 1.2 GB per year, storage should not be a

## Simplified Payment Verification

is possible to verify payments without running a full network the A user only needs to keep a copy of the block headers querying network nodes until he's convinced he has by ongest chain, and obtain the Merkle branch linking the
fansaction for himself, but by linking it to a place in the chain, he can see that a network node has accepted it, and block


As such, the verification is reliable as long as honest nodes overpowered by an aut is more vulnerable if the network is ransactions for themselves, the simplified method can be ooled by an attacker's fabricated transactions for as long as e attacker can continue to overpower the network. One etwork nodes when they detect an invalid block, prompting the user's software to download the full block and alerted transactions to confirm the inconsistency. Businesses that receive frequent payments will probably stir want to run their own nodes for more independent security and quicke verification
. Combining and Splitting Value
Although it would be possible to handle coins individually, it cent in a transfer. To allow value to be split and combined,
cor cent in a transfer. To allow value to be split and combined
ransactions contain multiple inputs and outputs. Normally there will be either a single input from a larger previous
transaction or multiple inputs combining smaller amounts, and transaction or multiple inputs combining smaller amounts, and at most two outputs: one for the payment, and one returning
the change, if any, back to the sender.

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should be noted that fan-out where a transacion depend on several transactions, and those transactions depend on many more, is not a problem here. There is never the need to 10. Privacy

The traditional banking model achieves a level of privacy by rriting access to information to the parties involved and the publicly precludes this method, but privacy can still be maintained by breaking the flow of information in another place: by keeping public keys anonymous. The public can see without information linking the transaction to anyone. This is similar to the level of information released by stock exchanges, where the time and size of individual trades, the
"tape", is made public, but without telling who the parties were.

## Identities $\quad$ Transactions $\rightarrow \underset{\substack{\text { Thusted } \\ \text { Thid Paty }}}{\text { Counteranty }} \xrightarrow{\text { Public }}$

## s an additional firewall, a new key pair should be used for

 each transaction to keep them from being linked to a common owner. Some linking is still unavoidable with multi-input ransactions, which necessarily reveal that their inputs were owned by the same owner. The risk is that if the owner of a belonged to the same owner.
## 11. Calculations

We consider the scenario of an attacker trying to generate an alternate chain faster than the honest chain. Even if this is changes, such as creating value out of thin air or taking money that never belonged to the attacker. Nodes are not going to accept an invalid transaction as payment, and honest can only try to change one of his own transactions to take back money he recently spent. The race between the honest chain and an attacker chain can be characterized as a Binomial Random Walk. The success event is the honest chain being extended by one block, increasing its lead by +1 , and the failure event is the attacker's chain being extended by one block, reducing the gap by -1 . The probability of an attacker catching up from a given deficit is analogous to a credit starts at a deficit and plays potentially an infinite number of trials to try to reach breakeven. We can calculate the probability he ever reaches breakeven, or that an attacker ever catches up with the honest chain, as follows [8]:
$p=$ probability an honest node finds the next block
$q=$ probability the attacker finds the next block $q_{z}=$ probability the attacker will ever catch up from $z$ blocks behind

$$
q_{z}=\left\{\begin{array}{cc}
1 & \text { if } p \leq q \\
(q / p)^{z} & \text { if } p>q
\end{array}\right\}
$$

Given our assumption that $p>q$, the probability drops exponentially as the number of blocks the attacker has to doesn't make a lucky lunge forward early on, his chances become vanishingly small as he falls further behind. We now consider how long the recipient of a new transaction needs to wait before being sufficiently certain the sender can't change
wants to make the recipient believe he paid him for a while, then switch it to pay back to himself after some time has the sender hopes it will be too late. The receiver generates a new key pair and gives the public key to the sender shortly chain of blocks ahead of time by working on it continuously until he is lucky enough to get far enough ahead, then executing the transaction at that moment. Once the transaction is sent, the dishonest sender starts working in secret on a parallel chain containing an alternate version of his ransaction. The recipient waits until the transaction has been added to a block and $z$ blocks have been linked after it. He made, but assuming the honest blocks took the average expected time per block, the attacker's potential progress will be a Poisson distribution with expected value:

$$
\lambda=z \frac{q}{p}
$$

To get the probability the attacker could still catch up now, we could have made by the probability he could catch up from that point:

$$
\sum_{k=0}^{\infty} \frac{\lambda^{k} e^{-\lambda}}{k!} \cdot\left\{\begin{array}{cl}
(q / p)^{(z-k)} & \text { if } k \leq z \\
1 & \text { if } k>z
\end{array}\right.
$$

Rearranging
distribution.

## $-\sum_{k=0}^{z} \frac{\lambda^{k} e^{-\lambda}}{k!}\left(1-(q / p)^{(z-k)}\right)$

Converting to C code
Converting to C c


Running some results, we can see the probability drop off exponentially with $z$.

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 $q=0$$P=0$
$P=0$
$P=0$
$q=0$

$=$
 Solving for P less than $0.1 \%$

| $\mathrm{q}=0.15$ | $\mathrm{z}=8$ | $\mathrm{q}=0.20$ | $\mathrm{z}=11$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{q}=0.35$ | $\mathrm{z}=41$ | $\mathrm{q}=0.40$ | $\mathrm{z}=89$ |

12. Conclusion

We have proposed a system for electronic transactions f coins made from digital started with the usual framework of coins made from digital signatures, which provides strong
control of ownership, but is incomplete without a way to prevent double-spending. To solve this, we proposed a peer-to-peer network using proof-of-work to record a public history of transactions that quickly becomes computationally impractical for an attacker to change if honest nodes control a majority of CPU power. The network is robust in its unstructured simplicity. Nodes work all at once with little coordination. They do not need to be identified, since messages are not routed to any particular place and only need
to be delivered on a best effort basis. Nodes can leave and ejoin the network at will, accepting the proof-of-work chain as proof of what happened while they were gone. They vote with their CPU power, expressing their acceptance of valid blocks by working on extending them and rejecting invalid blocks by efusing to work on them. Any needed rules and incentives an be enforced with this consensus mechanism.

## 3. References

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